

Find a solution (or solutions) that satisfies the KKT conditions for the following optimization problem:

$$\underset{x}{\text{minimize}} \quad f(x) = 2x_1 + x_2 \quad (1)$$

$$\text{subject to} \quad h(x) = x_1 + x_2 - 1 = 0 \quad (2)$$

$$g(x) = x_1 + 2x_2 - 2 \leq 0 \quad (3)$$

The KKT conditions are given by:

1. $\nabla_x \mathcal{L}(x^*, \lambda^*, \mu^*) = \nabla_x f(x) + \lambda^* \nabla_x h(x^*) + \mu^* \nabla_x g(x^*) = 0$

2. $\mu^* \geq 0$

3. $\mu^* g(x^*) = 0$

4. $g(x^*) \leq 0$

5. $h(x^*) = 0$